# **Spin Cavitronics: Spintronics Meets Microwave Cavity**

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**Introduction** Spin cavitronics is a newly developing interdisciplinary field that combines spintronics with cavity quantum electrodynamics, and its purpose is to realize quantum information processing via photon-magnon interaction. A typical configuration of spin cavitronics is a YIG sphere (magnetic insulator with low damping) inside a microwave cavity. Avoided level crossing of the transmission spectrum indicates the strong coupling between magnons and photons.

#### Simulation in time domain

Dynamics of spin precession inside the YIG sphere is governed by the Landau-Lifshitz-Gilbert equation

$$\frac{\partial \mathbf{m}}{\partial t} = -\gamma \mathbf{m} \times \mathbf{H}_{\mathbf{eff}} + \alpha \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$$

with eigenmode (Kittel mode)  $\omega_H = \gamma H$ 

Dynamics of the microwaves is governed by the Maxwell's equation

$$\mu_0 \varepsilon_0 \frac{\partial}{\partial t} \left( \varepsilon_r(\mathbf{r}) \frac{\partial \mathbf{A}}{\partial t} \right) + \mathbf{\nabla} \times \left( \mu_r^{-1}(\mathbf{r}) \mathbf{\nabla} \times \mathbf{A} \right) = 0.$$

with the constitutive relationship  $\mathbf{B} = \mu_0(\mathbf{H} + \mathbf{M})$ 

# Simulation in frequency domain

The time-dependent LLG equation can be written down in frequency domain in linear approximation

$$i\omega \mathbf{m} = \hat{\mathbf{z}} \times (\omega_M \mathbf{H} - \omega_K \mathbf{m} + i\alpha \omega \mathbf{m})$$

which can be transformed to the form  $\mathbf{m} = \mu_0 \overline{\zeta} \mathbf{H}$  indicating that the dynamics of magnetization can be treated as a material with special permeability

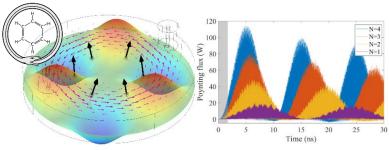
$$\overline{\mu}_{M} = \overline{\mathbf{I}} + \overline{\zeta} = \begin{pmatrix} 1 + u & -iv & 0 \\ iv & 1 + u & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$u = \frac{(\omega_{K} - i\alpha\omega)\omega_{M}}{(\omega_{K} - i\alpha\omega)^{2} - \omega^{2}}, \quad v = \frac{\omega\omega_{M}}{(\omega_{K} - i\alpha\omega)^{2} - \omega^{2}}.$$

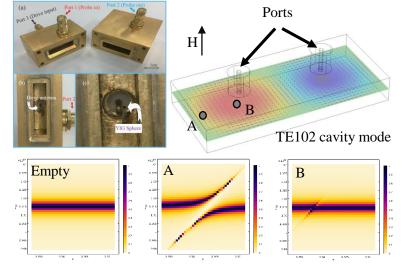
We can now simulate the hybrid system by solving only Maxwell's equations in frequency domain.

$$\nabla \times [\mu_r(\mathbf{r})^{-1} \nabla \times \mathbf{E}] - k^2 \varepsilon_r(\mathbf{r}) \mathbf{E} = 0$$

## Design of magnonic molecules

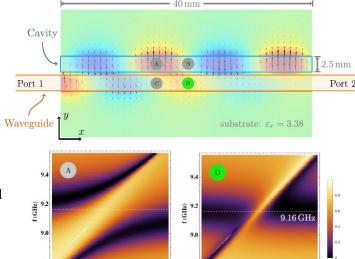
Each magnetic sphere can be treated as a magnonic atom, and multiple atoms form magnonic molecules mediated by cavity photons. Chiral magnonic molecules can be designed such as magnonic benzene with circulating photonic current.





### Prediction of attractive level crossing

Magnon-photon coupling usually gives rise to the level anti-crossing (level repulsion), where two levels repel to each other. By simulating the directional-coupler-like cavity, it's possible to induce an extra dissipative mode and realize novel attractive level crossings (level attraction).



#### Reference

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