

# **A Flow and Transport Model of Catalytic Multi-Pump Systems with Parametric Dependencies**

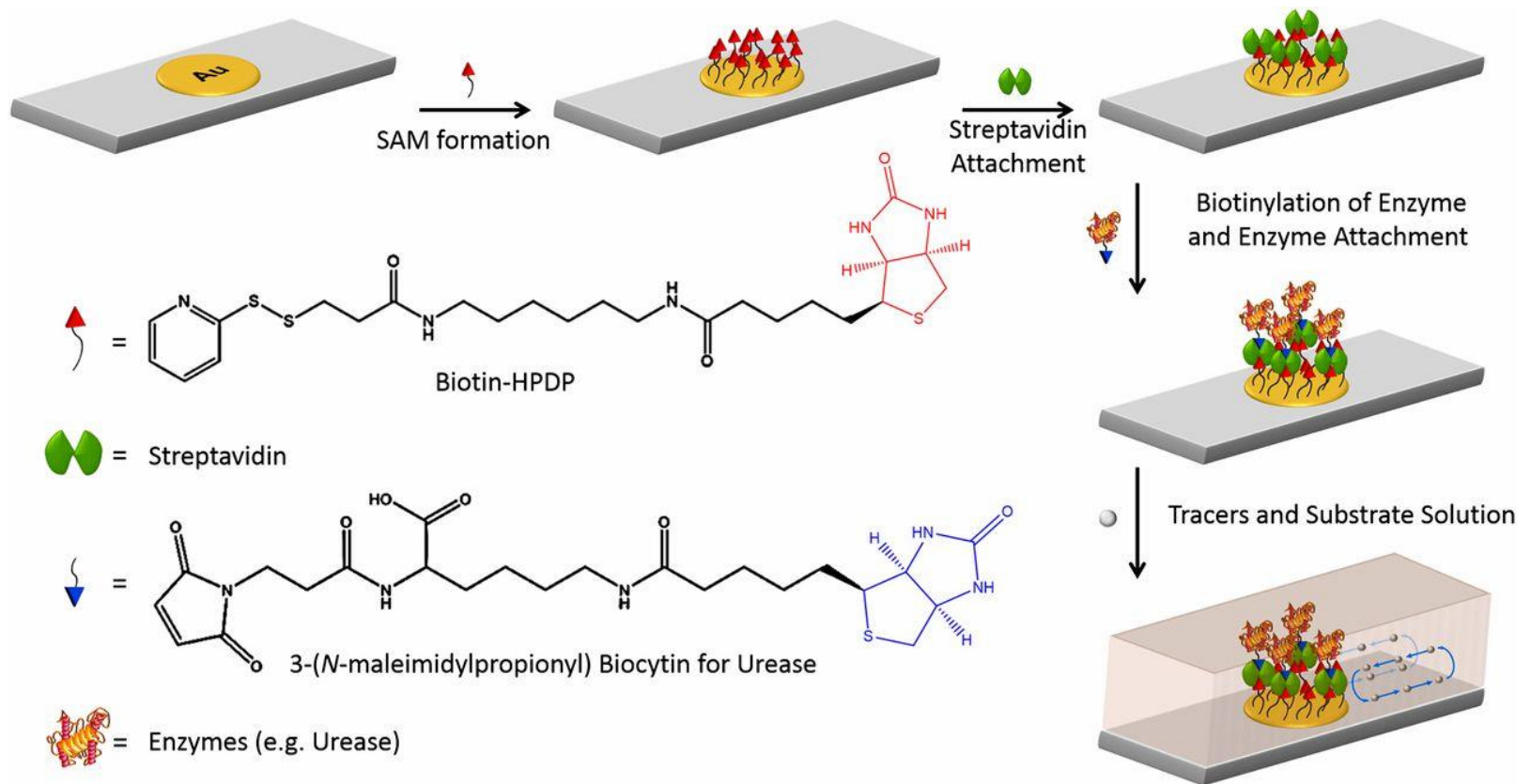
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# Introduction



Ortiz-Rivera, et al., Convective flow reversal in self-powered enzyme micropumps, PNAS, 113, 2585–2590 (2016)  
S. Sengupta, et al., Self-powered enzyme micropumps, Nat. Chem., 6, 415-422 (2014).

# Motivation

## Use for micropumps

- Microfluidic devices
- Non-pressurized fluid flow

## Future direction (multi-pumps)

- Imitation of biological systems
- Sensors
- Stimuli-response systems

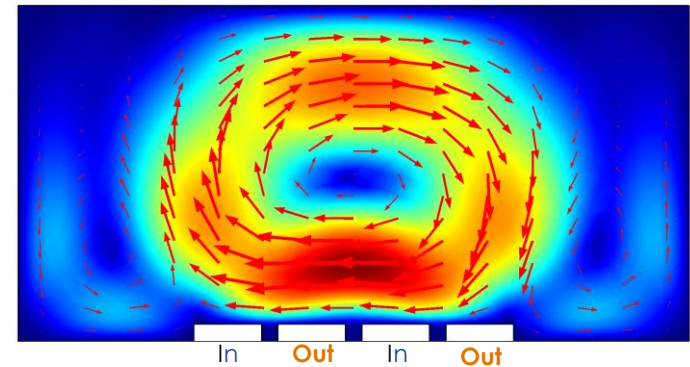
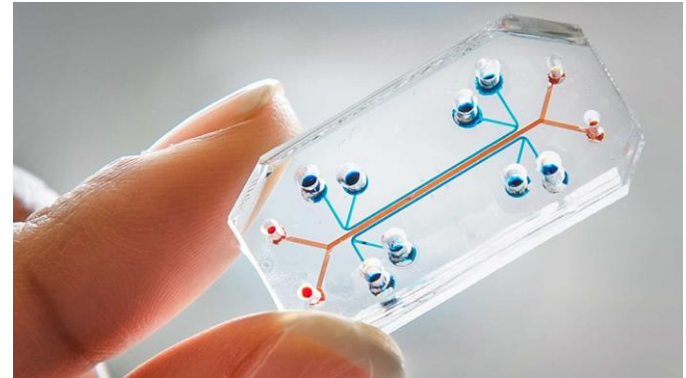


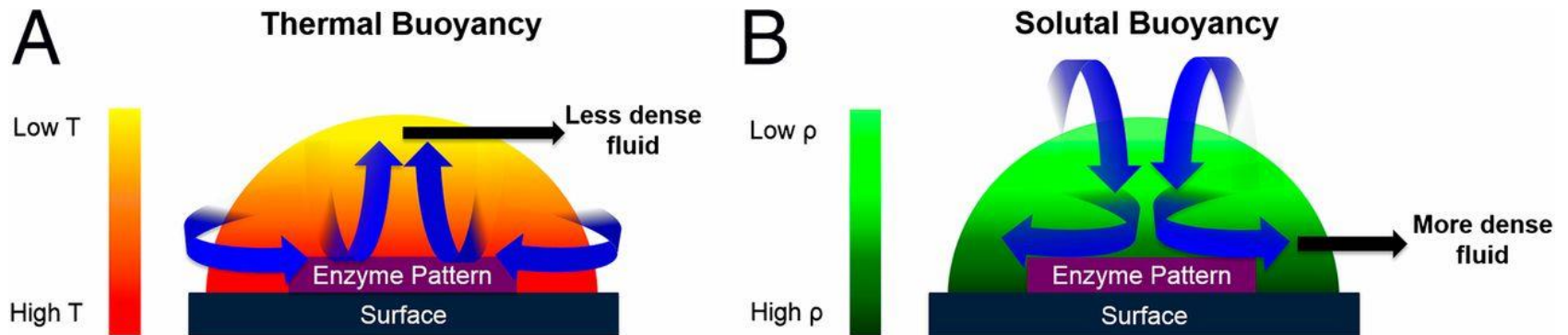
Image Source: <http://discovermagazine.com/media/Images/Issues/2015/june/organ-chip.jpg>

# Enzymes as Micro-pumps

## Thermally driven pumps

- Thermal coefficient of expansion
- Inward/outward

- Molar coefficient of expansion
- Inward/outward



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# Current Studies

Three parametric sweeps:

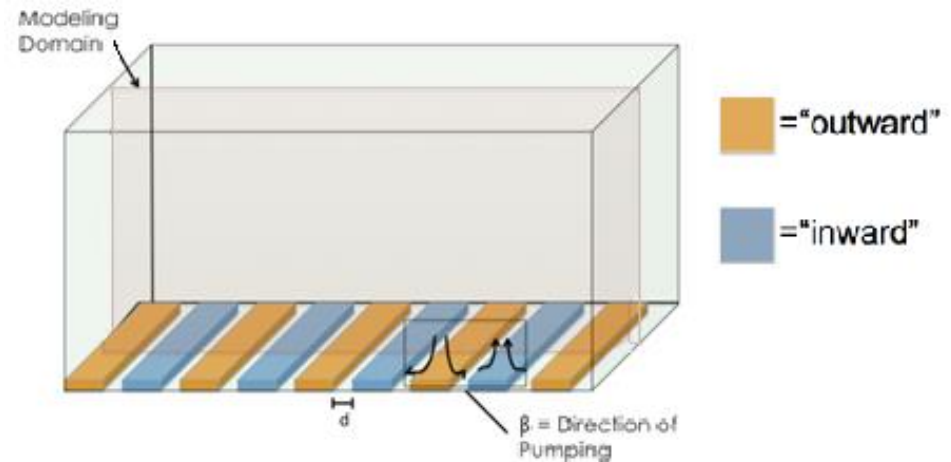
- Distance between pumps ( $d$ )
- Ratio of reaction rates ( $R$ )
- Direction of individual pumping ( $\beta$ )

$d = \text{Interpump distance}$

$$R = \frac{\text{Reaction rate of outward pump}}{\text{Reaction rate of inward pump}}$$

$\beta = \text{Volumetric Coefficient of Expansion}$

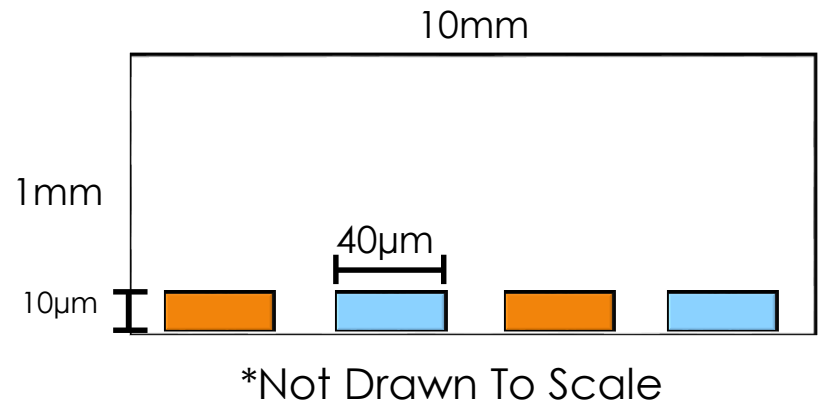
**The goal is to create a directed flow within the multi-pump system.**



# Modeling Procedures

Physics modules used:

- 0-Dimensional chemical engineering to space dependent model in a simplified 2-dimensional system
- Chemistry
- Transport of diluted species
- Laminar (creeping) flow



# Equations

Boussinesq approximation of the Navier-Stokes equation:

$$\rho \frac{\partial \mathbf{u}}{\partial t} = \nabla \cdot \left[ -p\mathbf{I} + \mu \left( \nabla \mathbf{u} + (\nabla \mathbf{u})^T \right) \right] + F,$$

$$F = -\rho_0 \tilde{g} \left( \sum \beta_{species} c_{species} \right)$$

$$\nabla \cdot \mathbf{u} = 0 \quad Re = \rho \mathbf{u} L / \mu$$

# Results: Spacing



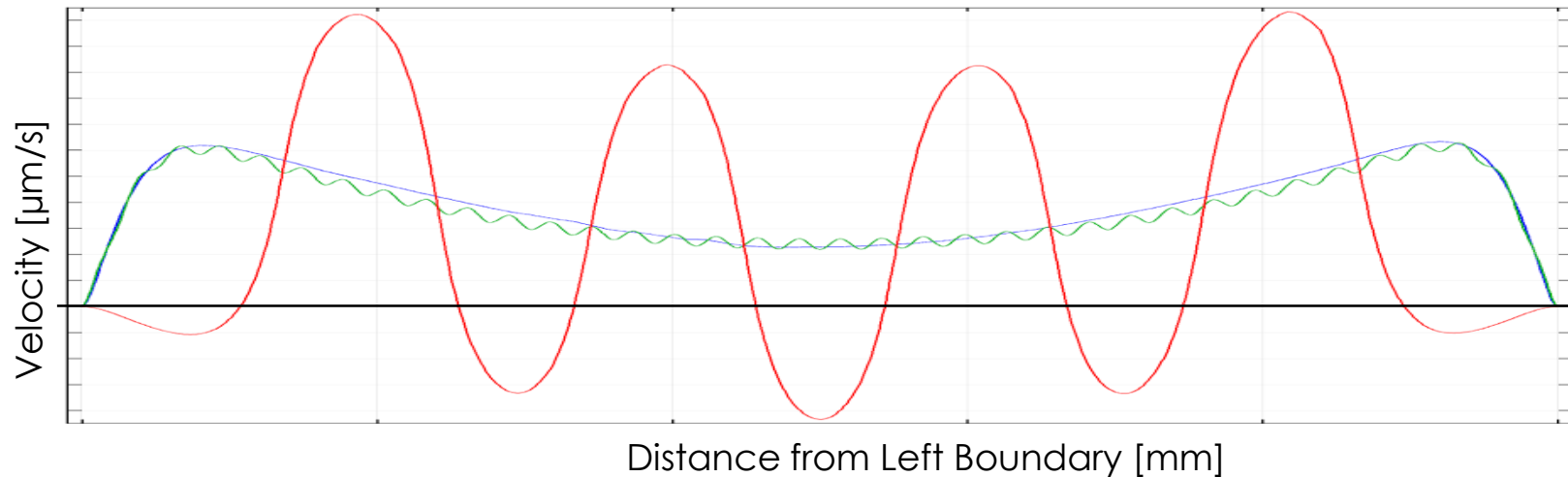
$d = 40\mu\text{m}$   
(Blue)



$d = 100\mu\text{m}$   
(Green)



$d = 1000\mu\text{m}$   
(Red)



- Constant parameters:
- $R=1$
  - First Pump = Outward
  - Last Pump = Inward
  - $t=100\text{min}$



# Results: Ratio of Reaction Rates



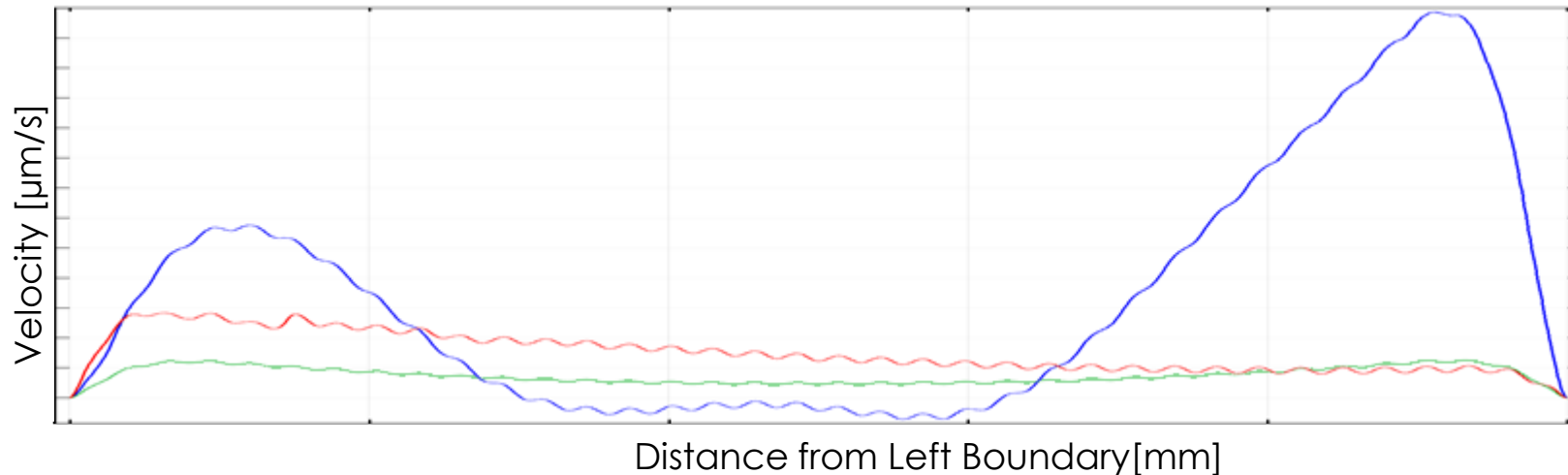
R = 0.2 (Blue)



R = 1 (Green)



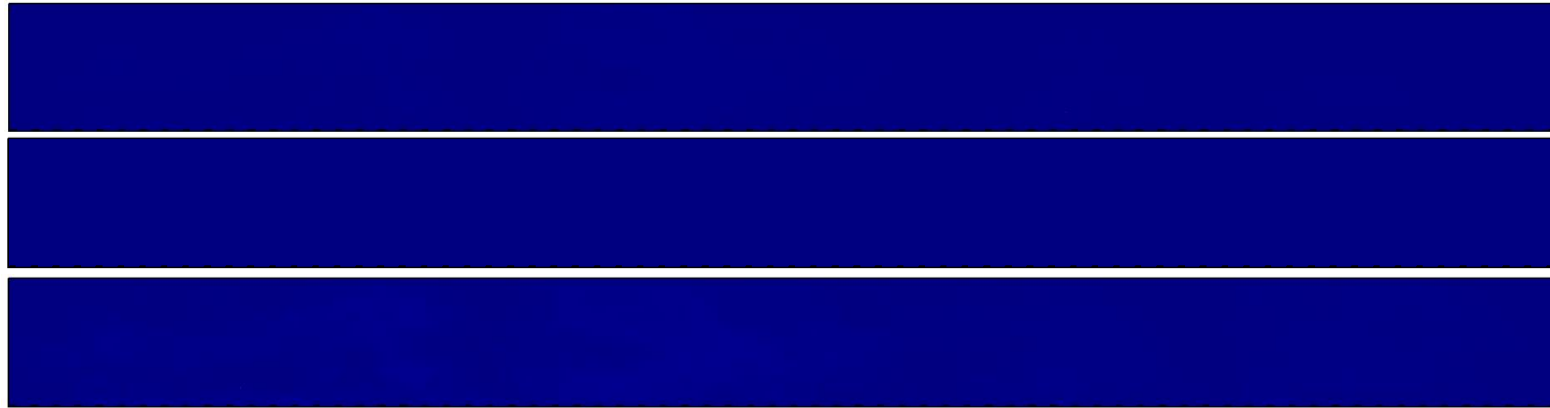
R = 5 (Red)



Constant parameters:

- $d = 100\mu\text{m}$
- First Pump = Outward
- Last Pump = Inward
- $t = 100\text{min}$

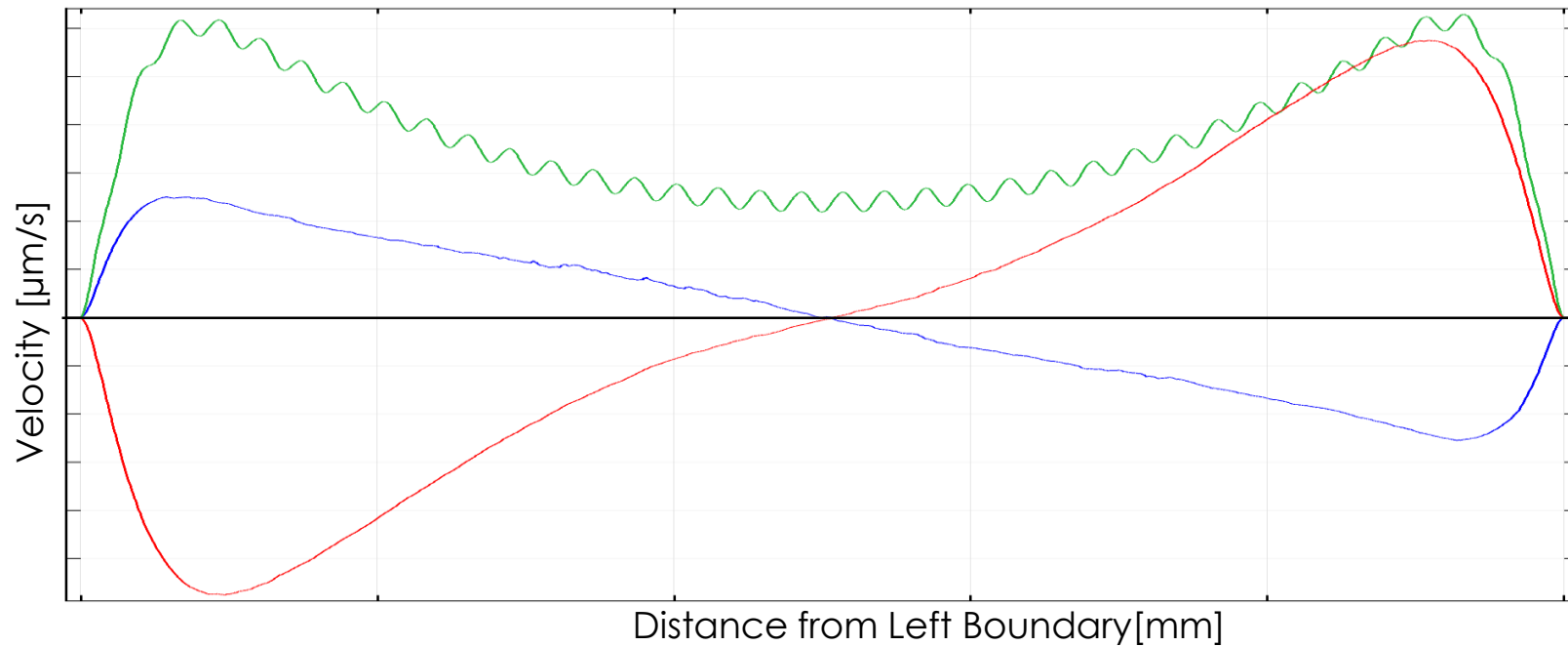
# Results: Direction of Pumping



Both Inward  
(Red)

First Pump Outward  
Last Pump Inward  
(Green)

Both Outward  
(Blue)



Constant parameters:

- $d = 100\mu\text{m}$
- $R = 1$
- $t = 100\text{min}$

# Conclusions

Multi-pump system shows continuous long-distance flows under the following conditions:

- Small spacing between pumps
- Reaction rate ratio of 1
- Alternating inward/outward pumps



# Acknowledgements



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CONFERENCE  
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# More Equations

Transport of dilute species:

$$\frac{\partial c_i}{\partial t} + \nabla \cdot (-D_i \nabla c_i) + \vec{u} \cdot \nabla c_i = R_i$$
$$N_i = -D_i \nabla c_i + \vec{u} c_i$$

Reaction rate calculations:

$$R_i = \frac{\tau_{max,i} c_i}{(K_{m,i} + c_i)} \text{ where } K_{m,i} = 1000[\mu\text{m}]$$

$$\tau_{max,i} = E k_{cat,i} M$$

where  $E$  = Concentration of Enzymes on Patch,

$M$  = Number of Active Sites per Enzyme

$$k_{cat,A} = 5E6 \left[ \frac{1}{s} \right] * R$$

$$k_{cat,B} = 5E6 \left[ \frac{1}{s} \right] * \left( \frac{1}{R} \right)$$

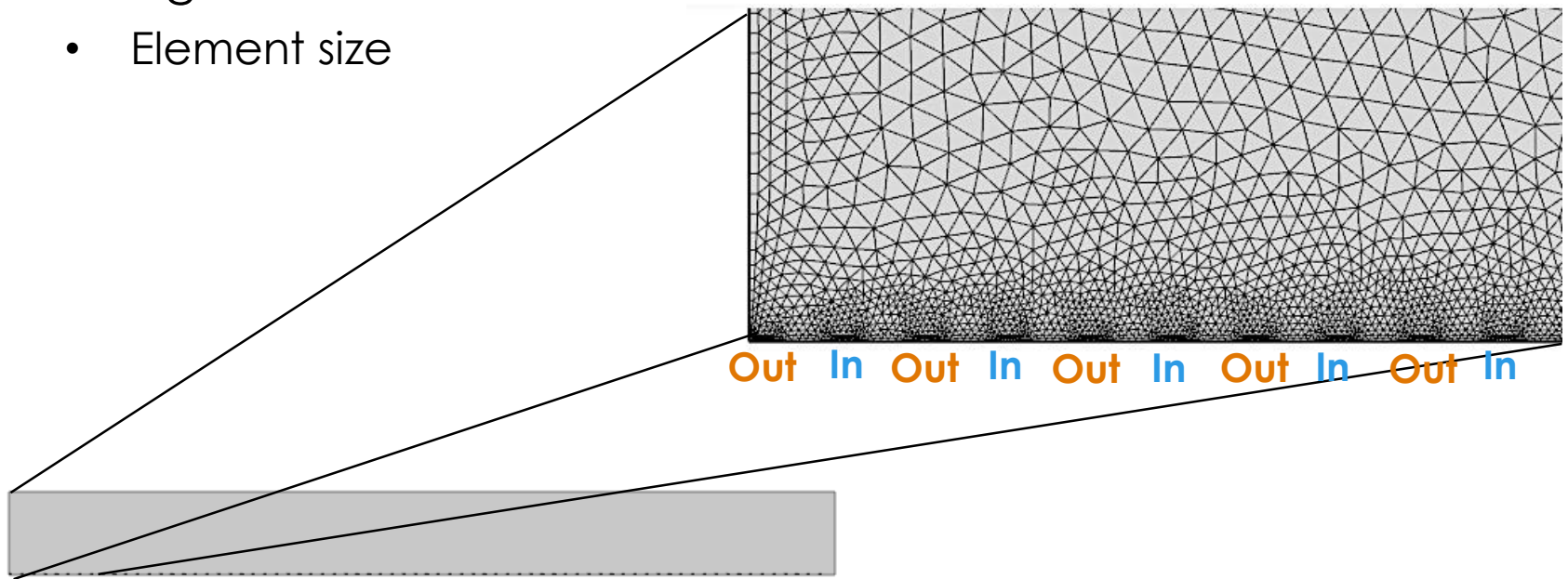
# More Modeling Procedures

## Geometry

- Dimensions
- Even number of pumps

## Meshing

- Element size



# Post-Processing

## Arrow surface

- Direction vectors of velocity
- Scaled by a factor of  $\sim 2000$

## Constant parameters

- Distance between pumps ( $d$ ) =  $100\mu\text{m}$
- Pump A outward/pump B inward
- Ratio of reaction rates ( $R$ ) = 1

