

# Coupling Forced Convection in Air Gaps with Heat and Moisture Transfer inside Constructions

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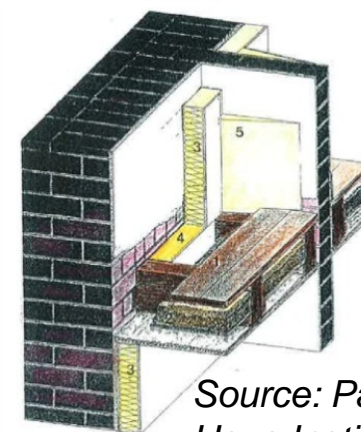
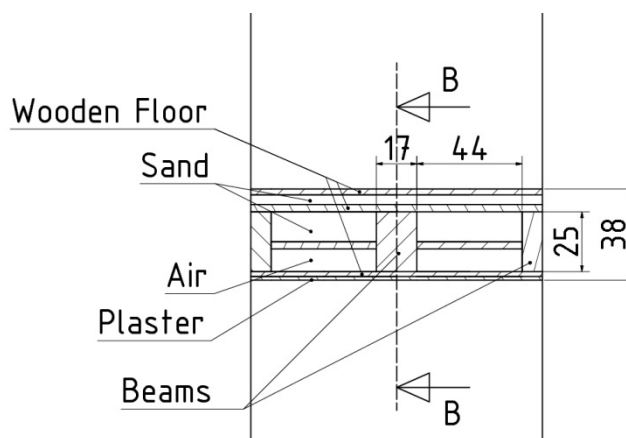
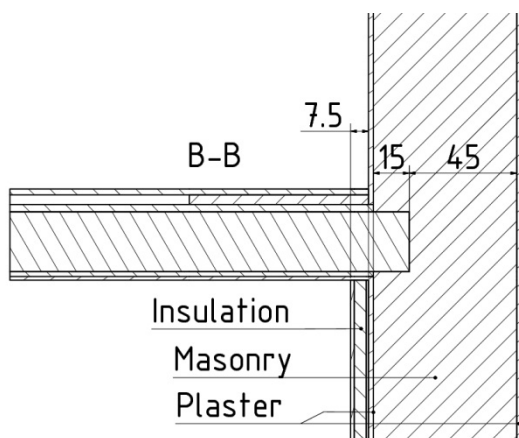
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- Simulation Modell
- Results

# Motivation

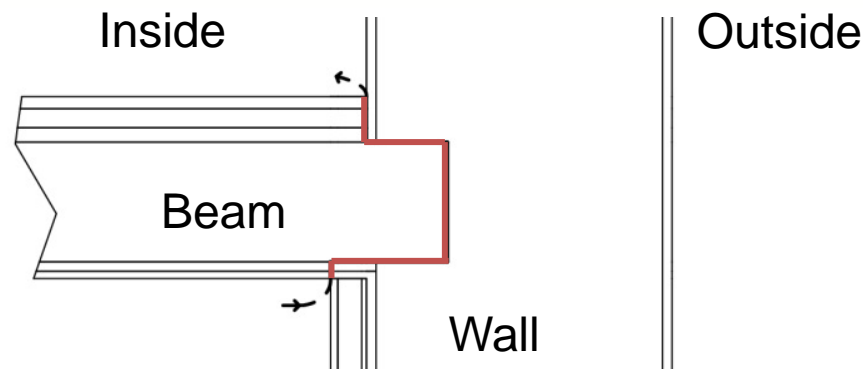


## EU Projekt 3ENCULT (WP3): Hygrothermal Simulation of Beam-Ends



Source: Passiv Haus Institut,  
Protokollband  
Nr.32, Architekt  
Fingerling

# Beam-End: Hygrothermal Simulation



- Heat and mass diffusion inside the solid domains
- Heat and mass convection through the air gap

# Heat and Mass Diffusion inside the Solid Domains

## PDE, Coefficient Form

$$\frac{\partial u}{\partial \varphi} \frac{\partial \varphi}{\partial t} + \nabla \cdot \left( -D_{m,\varphi} \nabla \varphi - D_{m,T} \nabla T \right) = 0$$

⇐ Moisture balance

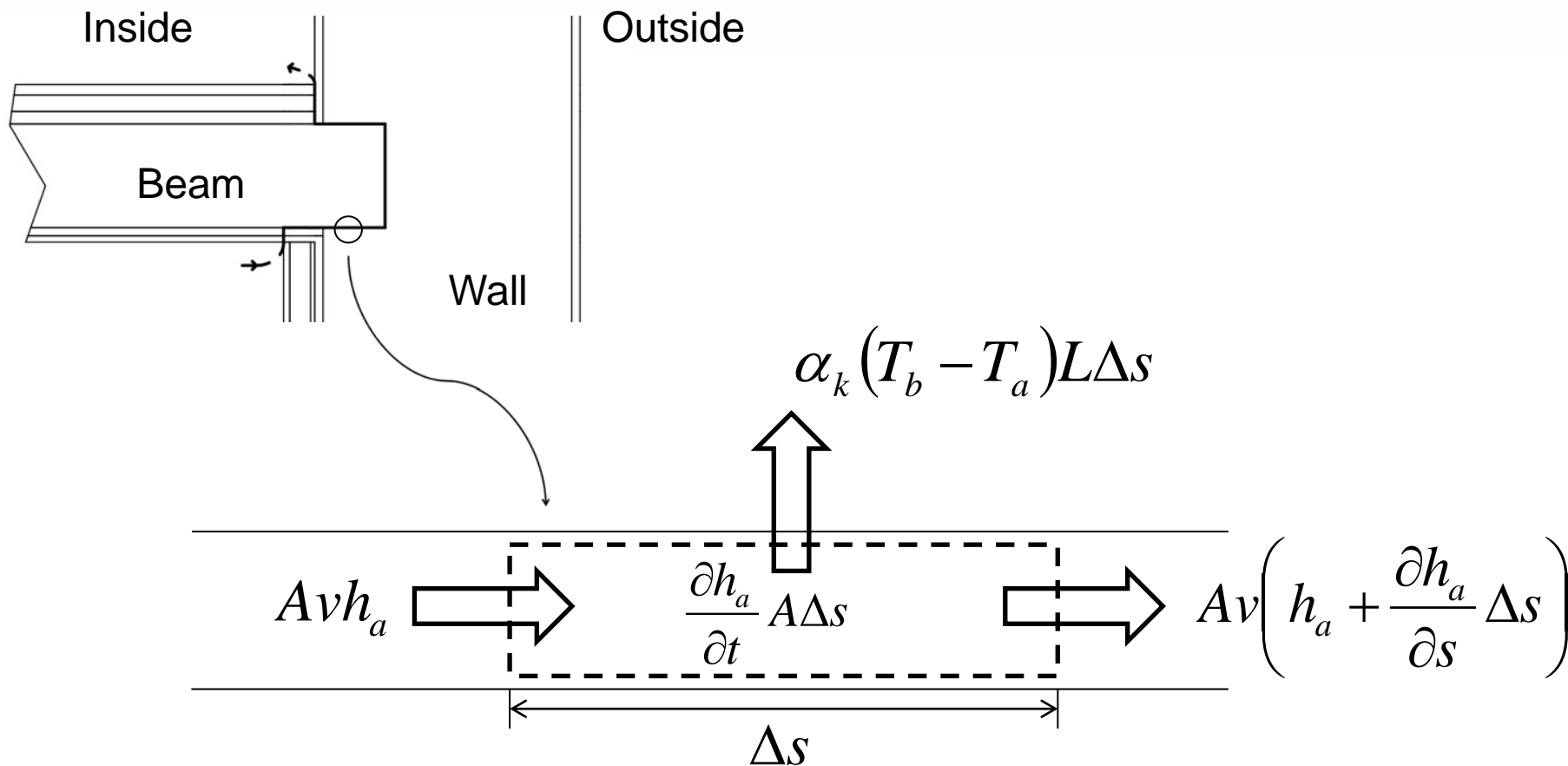
$$\frac{\partial h}{\partial T} \frac{\partial T}{\partial t} + \frac{\partial h}{\partial \varphi} \frac{\partial \varphi}{\partial t} + \nabla \cdot \left( -D_{e,T} \nabla T - D_{e,\varphi} \nabla \varphi \right) = 0$$

⇐ Energy balance

- ⇒
- Moisture distribution:  
 $\varphi(x,y,t)$  or  $a_w(x,y,t)$
  - Temperature distribution:  
 $T(x,y,t)$

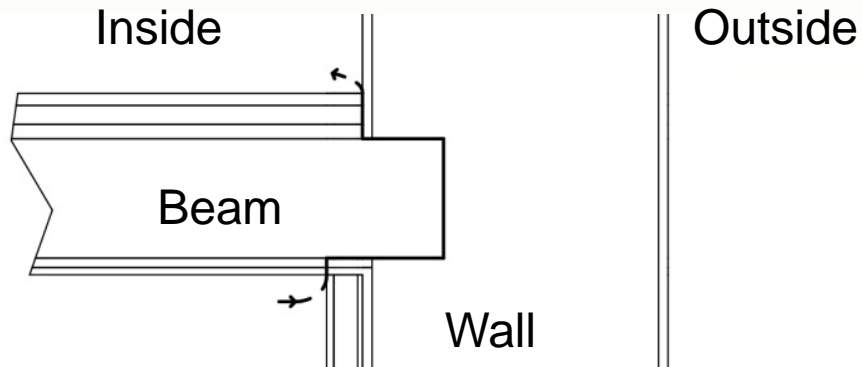
$\varphi$	Relative humidity
$T$	Temperature
$u$	Water content
$h$	Specific enthalpy

# Forced Convection in the Air Gap



Example: Energy Balance

## Forced Convection in the Air Gap: Governing Equations

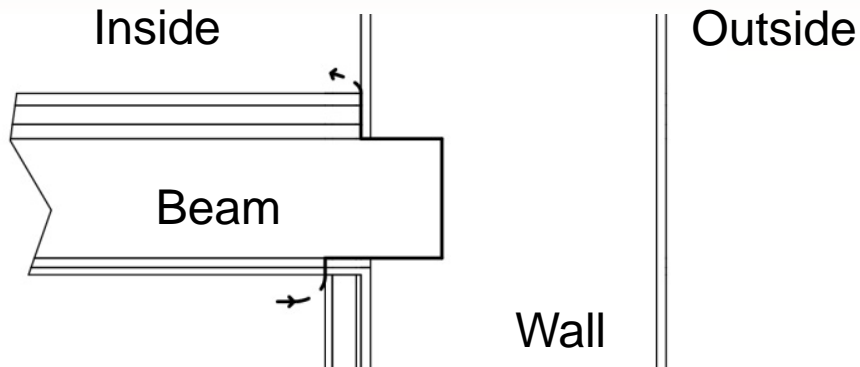


$\rho_v$	Vapor density
$h$	Air enthalpy
$A$	Cross section area
$L$	Cross section perimeter
$v$	Air velocity

$$A \left( \frac{\partial \rho_v}{\partial t} + v \frac{\partial \rho_v}{\partial s} \right) = L \beta_k (p_{v,b} - p_v) \quad \leftarrow \text{Moisture balance}$$

$$A \left( \frac{\partial h}{\partial t} + v \frac{\partial h}{\partial s} \right) = L \alpha_k (T_b - T) \quad \leftarrow \text{Energy balance}$$

# Weak Form on the Boundary



$w$	Test function
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$$\int_0^s \left\{ w \left[ \frac{\partial \rho_v}{\partial t} - \frac{L\beta_k}{A} (p_{v,b} - p_v) \right] - \frac{\partial w}{\partial s} v \rho_v \right\} ds + w v \rho_{v,s} - w v \rho_{v,0} = 0$$

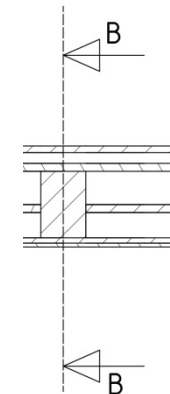
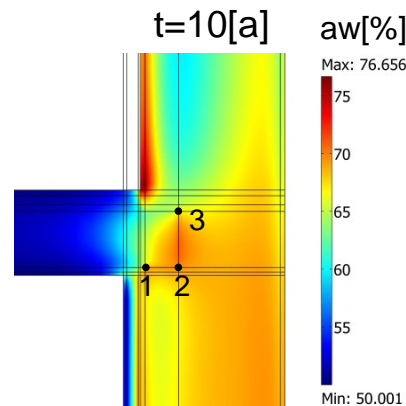
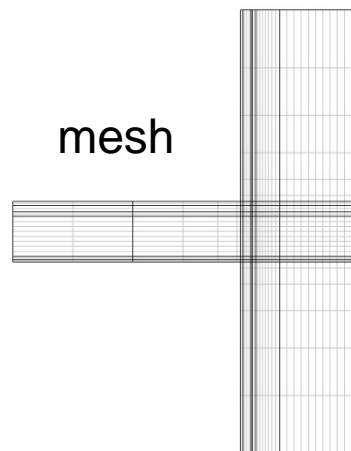
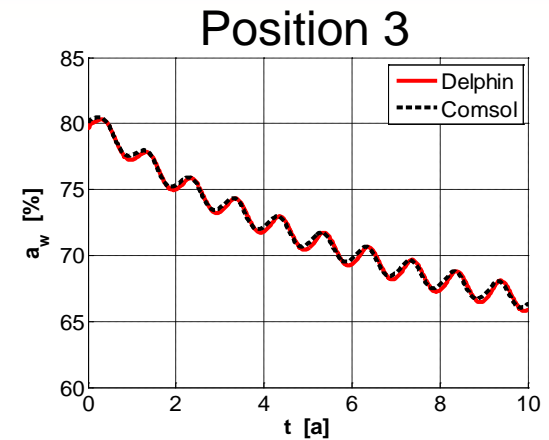
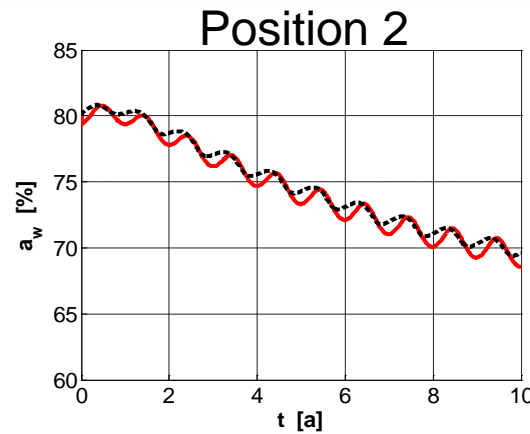
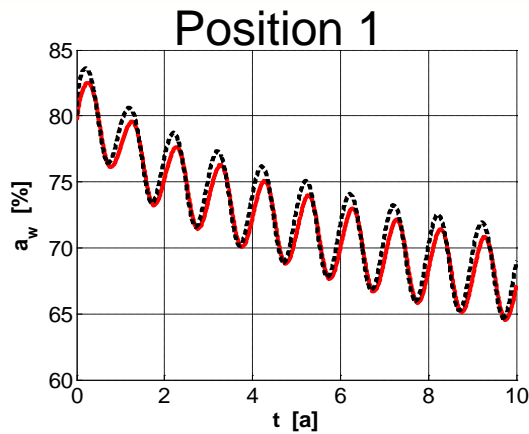
$$\int_0^s \left\{ w \left[ \frac{\partial h}{\partial t} - \frac{L\alpha_k}{Ac_p \rho} (h_b - h) \right] - \frac{\partial w}{\partial s} v h \right\} ds + w v h_s - w v h_0 = 0$$

Boundary Settings

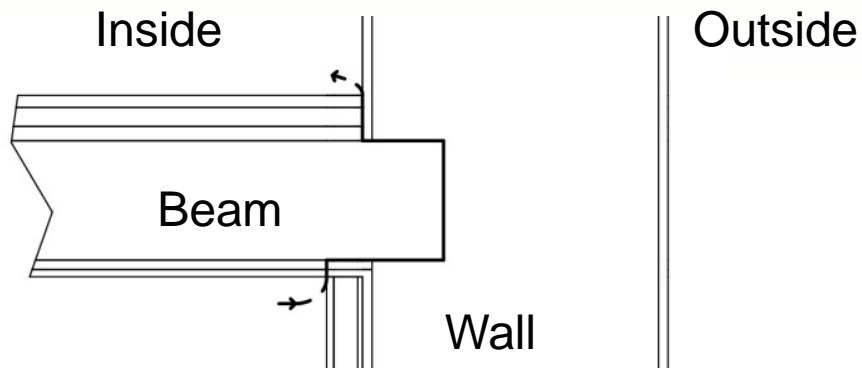
Point Settings



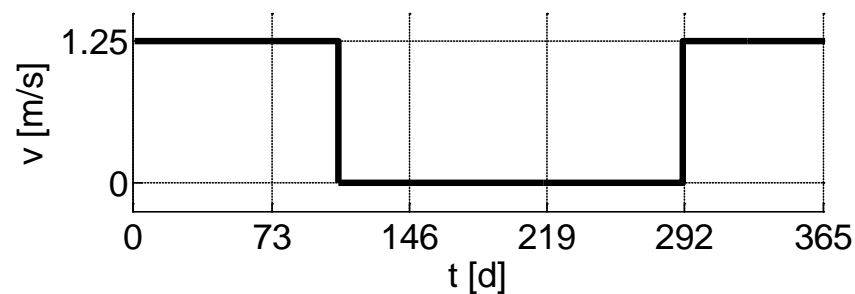
# Comparison with Delphin 2D Modell without Convection



# Forced Convection in the Air Gap: Air Velocity in the Gap

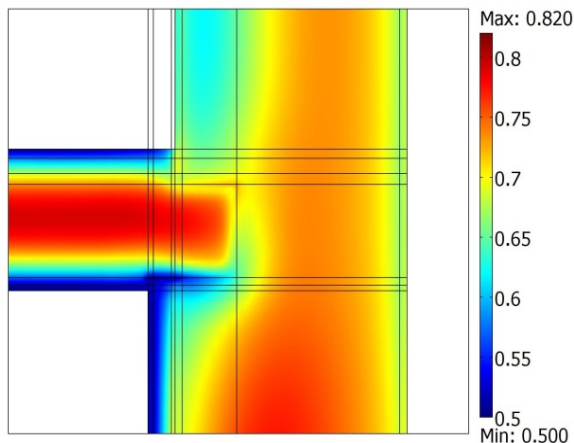


Development of the  
Air Velocity in the Gap

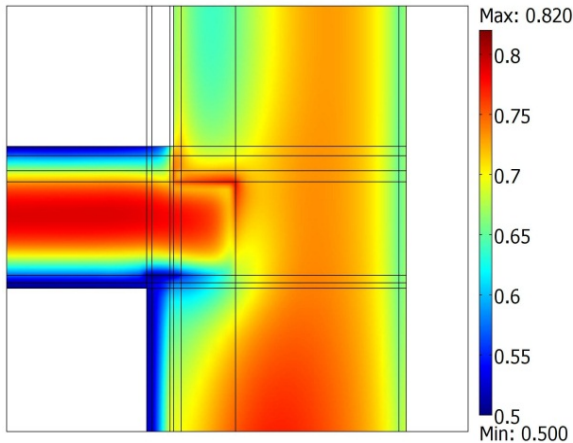


# Forced Convection in the Air Gap: Results

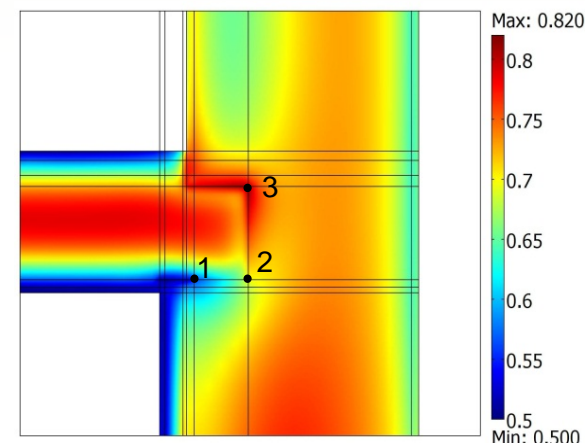
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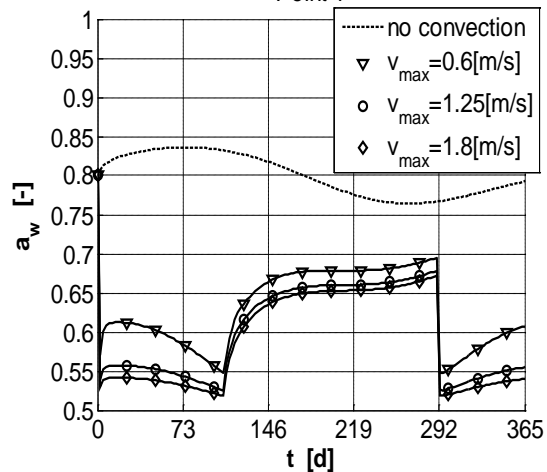
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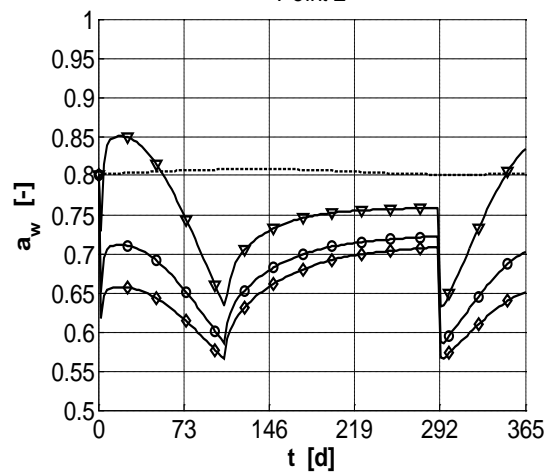
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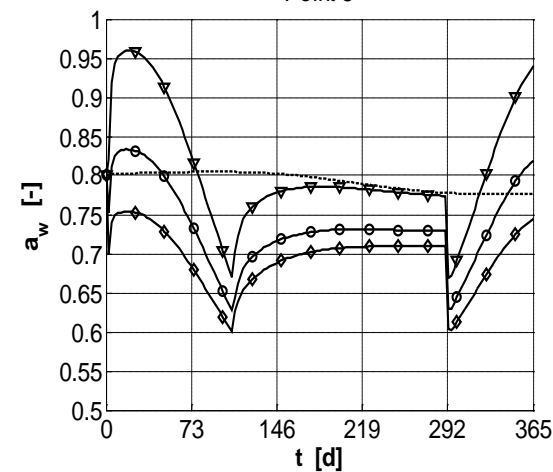
Point 1



Point 2



Point 3



# Outlook

## **Validation**

- Numerical error analysis
- Experimental validation

## **Further development**

- Free convection inside air cavities(CFD)

**Thank you for your attention!**

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